

DOCUMENT RESUME

ED 479 925

TM 035 229

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TITLE Replication of Major Profile Patterns in Structural Equation Modeling: Effect of Bootstrapping in a Small Sample.
PUB DATE 2002-04-00
NOTE 29p.; Paper presented at the Annual Meeting of the American Educational Research Association (New Orleans, LA, April 1-5, 2002).
PUB TYPE Reports - Research (143) -- Speeches/Meeting Papers (150)
EDRS PRICE EDRS Price MF01/PC02 Plus Postage.
DESCRIPTORS *Profiles; *Sample Size; *Structural Equation Models
IDENTIFIERS *Bootstrap Methods; *Replication

ABSTRACT

The effect of bootstrapping was studied by examining whether major profile patterns were replicated when sample sizes were reduced. Profile patterns estimated from the original sample (n=645) of the Wechsler Preschool and Primary Scale of Intelligence-Third Edition (WPPSI-III) Standardization Data were considered major profiles. For bootstrapping, the original sample was reduced to n=50, n=25, and n=20. From each reduced sample, profile patterns were extracted and compared to the major profile patterns. Then, the bootstrapping technique was applied to the reduced sample, and the bootstrap correlation matrix was estimated. Using the correlation matrix, profile patterns were estimated, and they were compared to the major profile patterns. To measure correspondence between the major profiles, correlation coefficients were computed. The profile patterns obtained from reduced samples without bootstrapping were poorly matched with the major profiles, whereas the profile patterns from bootstrapped samples were well matched with the major profile patterns. The bootstrapping substantially contributed to replicating major profiles when sample sizes were severely reduced. (SLD)

Running Head: Bootstrapping Effect

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Replication of Major Profile Patterns in Structural Equation Modeling:

Effect of Bootstrapping in a Small Sample

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Paper prepared for SIG: Structural Equation Model at the American Educational Research
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Abstract

The effect of bootstrapping was studied by examining whether major profile patterns were replicated when sample sizes were reduced. Profile patterns estimated from the original sample ($N = 645$) of WPPSI-III Standardization Data were considered major profiles. For bootstrapping, the original sample was reduced to $n = 50$, $n = 25$, and $n = 20$. From each reduced sample, profile patterns were extracted and compared to the major profile patterns. Then, the bootstrapping technique was applied to the reduced sample and the bootstrap correlation matrix was estimated. Using the correlation matrix, profile patterns were estimated and they were compared to the major profile patterns. To measure correspondence between the major profiles and the estimated profiles, correlation coefficients were computed. The profile patterns obtained from reduced samples without bootstrapping were poorly matched with the major profiles, whereas the profile patterns from bootstrapped samples were well matched with the major profile patterns. The bootstrapping substantially contributed to replicating major profiles when sample sizes were severely reduced.

Replication of Major Profile Patterns in Structural Equation Modeling:

Effect of Bootstrapping in a Small Sample

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This paper was designed to explore how much bootstrapping could help replicate major profile patterns when sample sizes were reduced from the original sample. Little research has been done about how effectively bootstrapping replicates factor structures of a population when a small sample is analyzed. It is generally known that estimates from a small sample may not be an appropriate representative of population characteristics of interest because the sample may not include all possible aspects of population characteristics. Similarly, factor structures estimated from the small sample may not represent true factor structures in a population and moreover, when a sample size gets smaller, representation of the population gets even worse. However, collecting a larger sample to fix such a problem is always expensive and time consuming. For this reason, the bootstrapping technique was introduced in the study.

The bootstrapping procedure creates pseudo replicate datasets by resampling. The procedure starts by selecting at random one case from a designated sample for bootstrapping; a user documents the case, returns it to the sample, randomly selects another case, documents its score, returns it to the sample, and so on. The step is repeated until the size of the first bootstrap sample reaches the same size as the original sample. Since the bootstrapping procedure is based on the purely random sampling (i.e., replacement is allowed), this random procedure allows all possible combinations of data structure that one can think of. For example, there are four

observations, A, B, C, and D. If these four observations are bootstrapped, the 1st bootstrap sample could be D, C, B, A. The first observation of the original sample now becomes the last observation in the bootstrap sample. The 2nd bootstrap sample could be A, B, A, B. In this bootstrap sample, the 1st and 2nd observations are the same as those of the original sample, but the 3rd and 4th are the same as the 1st and 2nd observations in the original sample. Or one can think of (A, A, A, A), ..., (D, D, D, D) since the chance of being selected is all the same ($p = .25$) for each. Again, this random procedure provides all possible combinations of data structure over and above the data structure of the original sample. This is the key concept of why the bootstrap procedure was implemented for the present study.

For this study, bootstrapping was not applied to the original sample, but from the original sample ($N = 645$) three samples (e.g., $n = 50$, $n = 25$, and $n = 20$) were randomly selected and then bootstrapping was applied to the reduced samples. The beauty of the bootstrap method is that as many samples as the user wants can be generated. Efron and Tibshirani (1993, p.52) suggest around 200 bootstrap samples for estimating standard errors and about 1000 bootstrap samples for empirical confidence intervals, but they do not include any recommended sample sizes regarding replicating factor structures in a population (since factor analysis is not popular in the Mathematical Field). An arbitrary number, 500 between 200 and 1000 was chosen, and 500 bootstrap samples were generated from each of the reduced samples. However, there is no reason to fix this number for replicating the present study as the number of bootstrap samples depends solely on sample characters for factor structure studies.

From each of the reduced samples (sample sizes $n = 50$, $n = 25$, or $n = 20$, respectively), 500 correlation matrices were computed, and then a mean correlation matrix of the 500 matrices was estimated. All these procedures were done by PRELIS 2 (Joreskog & Sorbom, 1996). With the mean correlation matrix, principal component analysis (PCA), multidimensional scaling (MDS), and confirmatory factor analysis (CFA) were conducted. The results of PCA and MDS were compared with the results from analyses of the original sample ($N = 645$). To inspect behaviors of profile patterns, coordinates of PCA and MDS from bootstrap correlation matrices were superimposed on those of the original sample. To quantify magnitude of correspondence between estimated profiles by bootstrapping and major profiles, (Pearson Product Moment) correlation coefficients were used.

Method

The data used in this study was collected with the Wechsler Preschool and Primary Scale of Intelligence – Third Edition (WPPSI-III) Standardization Sample (Wechsler, 2002). The subtests used in the study consist of the Similarities (SI), Vocabulary (VC), Word Context (WC), Block Design (BD), Matrix Reasoning (MR), and Picture Concepts (PCO). Verbal Similarities and Vocabulary subtests are traditionally considered components of Verbal IQ (VIQ), but Word Context is a new subtest for VIQ. The last three subtests, Block Design, Matrix Design, and Picture Concepts are considered components of Performance IQ (PIQ). The Block Design and Matrix Reasoning are traditionally considered components of PIQ, but Picture Concepts subtest is a new PIQ subtest. Accordingly, a two-factor model is proposed: the VIQ vs. PIQ factors. The data for this study were collected by The Psychological Corporation and are a subset of the 1534 girls and boys who were collected in the WPPSI-III standardization sample. The age range

of the standardization sample is from 2 to 7 years old, but the range for this study is 5 to 7 years old. The composition of gender is $n = 316$ (49%) for girls and $n = 329$ (51%) for boys.

For an exploratory Principle Component Analysis (PCA), correlation matrices were used. For PAMS, a nonmetric MDS was used to analyze these correlations. Since $\delta_{tt'}^2 = (1 - r_{tt'})$ (see p.105, Davison, 1993), where t and t' refer to subtests, dissimilarity between two tests is inversely related with correlation. For PAMS approach, correlations were converted into dissimilarities and the dissimilarities were entered for the analysis. Table 1 shows the intercorrelations of the six intelligence subtests and Table 2 shows the coordinates from PAMS and 2nd PC and these coordinates were estimated from the same correlation matrix of $N = 645$.

Insert Table 1 and Table 2 about here.

The sample size sample size $N = 645$ was radically reduced to $n = 50$, $n = 25$, $n = 20$ to examine whether bootstrapping can help replicate the major profile patterns from the reduced samples. Each of the reduced samples for bootstrapping was randomly selected from the original sample ($N = 645$) and 500 bootstrap samples were generated from the sample. The sample designated for bootstrapping was considered to be a finite bootstrap population.

Inter-subtest correlation matrices were computed from five hundred bootstrap samples and then a mean correlation matrix from the five hundred correlation matrices was estimated. This mean-correlation matrix was eventually used for PCA, PAMS, and confirmatory factor analyses. A confirmatory factor analysis, based on the same intercorrelations used in the

exploratory PCA and PAMS approach, was performed through LISREL 8 (Joreskog & Sorbom, 1993) on the six subtests of the WPPSI-III. The hypothesized model based on the original sample ($N = 645$) is presented in Figure 1 where circles represent latent variables, and rectangles represent observed variables (or subtests).

 Insert Figure 1 about here.

A two-factor model of “Intelligence” was hypothesized. The first factor is VIQ which corresponds to the negative sides in the PAMS model and the second factor is PIQ which corresponds to the positive sides in the PAMS model, is hypothesized. Considering characters of intelligence, the first factor is left free to be correlated with the second factor.

Results

Principal Component Analysis

To examine a factor structure, principle component analyses (PCA) was conducted for all samples with two-factor solution. The first principal component was ignored since it represents general ability or item difficulty factor, and had all substantial positive loadings as expected. Therefore, only the second component was examined. Using the bootstrap mean correlation matrix, PC was conducted. Table 3 summarized coordinate values of the second principal component estimated from NOT bootstrapped samples and BOOTSTRAPPED samples.

 Insert Table 3 about here.

PAMS

To examine profile patterns, PAMS was conducted for all four samples used in the study. Since $(1 + K)$ factor solution but the general factor in PCA corresponds K dimensional solution in MDS (see Davison, 1985 or Kim & Davison, 2001), one-dimensional solution was desired. Using the same mean correlation matrix used in PC, PAMS was conducted. Table 4 summarized coordinates of the dimension extracted from non bootstrapped samples as well as bootstrapped samples.

 Insert Table 4 about here.

The table included the one-dimensional solution resulting from a nonmetric MDS analysis of the correlations among WPPSI-III Intelligence Subscales. The dimension had two sides; negative and positive. The negative side representing VIQ consisted of Similarities, Vocabulary, and Word Context. The positive side representing PIQ contained Block Design, Matrix Reasoning, and Picture Concepts. The dimension that includes VIQ and PIQ was labeled General Ability dimension.

Confirmatory Factor Analysis

Maximum likelihood estimation was employed to estimate all models. The hypothesized model (see Figure 1) using the original data ($N = 645$) was tested without inclusion of error covariances among observed variables (or subtests) and was supported for the model, $\chi^2(8, N = 645) = 10.84$, $P\text{-value} = 0.21$, $RMSEA = 0.02$, ($AIC = 36.84$ vs. Saturated $AIC = 42.00$), $ECVI = 0.057$, and $GFI = 0.99$. The model based on the sample data with $n = 50$, but using the bootstrap mean correlation matrix, was tested and supported for the model, $\chi^2(8, n = 50) = 3.61$, $P\text{-value} = 0.89$, $RMSEA = 0.00$, ($AIC = 29.61$ vs. Saturated $AIC = 42.00$), $ECVI = 0.69$, and $GFI = 0.98$. The model based on the sample data with $n = 25$, but using the bootstrap mean correlation matrix, was tested but not supported for the model, $\chi^2(8, n = 25) = 16.34$, $P\text{-value} = 0.04$, $RMSEA = 0.21$, ($AIC = 42.34$ vs. Saturated $AIC = 42.00$), $ECVI = 1.76$, and $GFI = 0.82$. The model based on the sample data with $n = 20$, but using the bootstrap mean correlation matrix, was tested and supported for the model, $\chi^2(8, n = 20) = 8.57$, $P\text{-value} = 0.38$, $RMSEA = 0.06$, ($AIC = 34.57$ vs. Saturated $AIC = 42.00$), $ECVI = 1.82$, and $GFI = 0.87$. Figures 2, 3, and 4 represent the path diagrams of the confirmatory factor analyses based on the bootstrap mean correlation matrices.

 Insert Figures 2, 3, & 4 about here.

Relationship Between Major Profile and Reduced Sample Profile

To inspect profile patterns, coordinates of PCA and MDS were plotted. Before bootstrapping was applied, the profiles estimated from reduced samples fell into different patterns from the major profile, but after bootstrapping, the profile patterns became similar to the major profile pattern. Moreover, to quantify correspondence between major profiles and estimated profiles from the samples, correlation coefficients were used.

First, profile patterns of PCA coordinates were examined. The correlation between the major profile and the profile of non-bootstrapped samples ($n = 50$, $n = 25$, and $n = 20$) was computed: $Cor(N = 645, n = 50) = 0.72$, $Cor(N = 645, n = 25) = 0.10$, and $Cor(N = 645, n = 20) = 0.75$. None of the correlations were statistically significant and the mean correlation was 0.52. Figure 5 represents PC profile patterns of non-bootstrapped samples.

Insert Figure 5 about here.

The correlation between the major profile and the profile of bootstrapped samples ($Bn = 50$, $Bn = 25$, and $Bn = 20$) was examined. $Cor(N = 645, Bn = 50) = 0.85^*$, $Cor(N = 645, Bn = 25) = 0.85^*$, and $Cor(N = 645, Bn = 20) = 0.94^{**}$. All of the coefficients were statistically significant at $\alpha = .05$ and the mean correlation was 0.88. Figure 6 shows PC profile patterns of bootstrapped sample.

 Insert Figure 6 about here.

Second, profile patterns of MDS coordinates were examined. The correlation between the major profile and the profile of non-bootstrapped samples ($n = 50$, $n = 25$, and $n = 20$) was computed: $Cor(N = 645, n = 50) = 0.17$, $Cor(N = 645, n = 25) = 0.02$, and $Cor(N = 645, n = 20) = 0.05$. None of the correlations were statistically significant and the mean was 0.08. Figure 7 represents MDS profile patterns of non-bootstrapped samples.

 Insert Figure 7 about here.

The correlation between the major profile and the profile of bootstrapped samples ($Bn = 50$, $Bn = 25$, and $Bn = 20$) was examined: $Cor(N = 645, Bn = 50) = 0.88^*$, $Cor(N = 645, Bn = 25) = 0.87^*$, and $Cor(N = 645, Bn = 20) = 0.79^{ns}$. The first two coefficients were statistically significant at $\alpha = .05$, but the last one was not. The overall mean was 0.85. Figure 8 represents MDS profile patterns of bootstrapped samples.

 Insert Figure 8 about here.

Discussion

The bootstrapping helped replicate the major profile pattern when the sample size was tremendously reduced from the original sample. When $n = 50$, PC and PMS coordinates of non-bootstrapped sample had the same direction as those of bootstrapped sample. The negative side included all VIQ subtests and the positive side contained all PIQ subtests, and the direction was consistent with the direction of the original sample's ($N = 645$) coordinates. However, when $n = 25$ and $n = 20$, the directions of PC and PAMS coordinates of non-bootstrapped samples were not consistent with the direction of the original sample coordinates. On the other hand, the bootstrapped sample coordinates of the same size ($n = 25$ or $n = 20$) were consistent with those of the original sample. Therefore, in this case, estimated factor structure of the bootstrapped sample can be informative, but the result from non-bootstrapped sample may be misleading.

To replicate the profile pattern (or factor structure) obtained from the bootstrapped samples based on the bootstrap mean matrices, the confirmatory factor analyses were conducted and their model fits were examined. The results from the bootstrapped samples $n = 50$ and $n = 20$ provided good model fits: $P\text{-value}=0.89$ and $\text{RMSEA}=0.00$ for $n = 50$ and $P\text{-value}=0.38$ and $\text{RMSEA}=0.06$ for $n = 20$. However, the results from the bootstrapped sample, $n = 25$ (e.g., $P\text{-value}=0.04$ and $\text{RMSEA}=0.21$), were not as good as the results of the other bootstrapped samples. Why?

There are a couple of explanations. First, the sample from the original data ($N = 645$) was a bad sample that did not include characteristics of the original factor structure. Second, the 500 bootstrap samples may not be large enough to replicate the original factor structure. To examine the first presumption, descriptive statistics of the original data and the sample size $n = 25$ were inspected. For $N = 645$, $\underline{M}(\text{SI}) = -0.02$, $\underline{M}(\text{VC}) = -0.01$, $\underline{M}(\text{WC}) = 0.01$, $\underline{M}(\text{BD}) = 0.02$,

$\underline{M}(\text{MR}) = 0.01$, and $\underline{M}(\text{PCO}) = 0.00$ and their standard deviations, 1.00, 1.00, 0.99, 1.00, 1.01, and 1.00, respectively. For $n = 25$, $\underline{M}(\text{SI}) = 0.215$, $\underline{M}(\text{VC}) = 0.142$, $\underline{M}(\text{WC}) = 0.20$, $\underline{M}(\text{BD}) = 0.10$, $\underline{M}(\text{MR}) = -0.04$, and $\underline{M}(\text{PCO}) = -0.10$ and their standard deviations, 0.96, 1.20, 0.92, 1.02, 1.20, and 1.05, respectively. This examination shows that central tendency and dispersion are different from each other in these two samples ($N = 645$ and $n = 25$).

To examine the second presumption, the number of bootstrap samples increased from $B=500$ (which was the bootstrap number used in the study) to $B=1000$, $B=2000$, $B=3000$, and $B=5000$ and bootstrap mean correlation matrices were estimated from the increased bootstrap samples. Note that “B” represents the number of bootstrap samples. Based on the mean correlation matrices, confirmatory factor analyses were performed and their model fits were examined.

When $B=1000$ mean correlation matrix was analyzed, P-value for the chi-square is 0.00 and RMSEA=0.28. These results did not improve from those of the $B=500$ analysis (whose P-value=0.04 and RMSEA=0.21). When the $B=2000$ mean correlation was used, P-value=0.15 and RMSEA=0.14 were obtained. These results showed improvement. When the $B=3000$ and $B=5000$ mean correlation matrices were analyzed, P-value=0.07 and RMSEA=0.19 and P-value=0.09 and RMSEA=0.17 were obtained, respectively. These results were consistent with those of the $B=2000$ correlation analysis. The increased number of bootstrapping did help recover the original factor structure.

Considering the comparison of descriptive statistics (between $N = 645$ and $n = 25$) and effect of increased number of bootstrap samples, it is interesting to notice that regardless of the difference in descriptive statistics between the two samples, the increment of bootstrap sample

number resulted in improvement of the model fit. In other words, the bootstrapping effect overpowered the distribution of a sample.

To reaffirm this proposition, all descriptive statistics of $n = 50$ and $n = 20$ were also checked. Their means and standard deviations were not identical to those of $N = 645$. The grand mean (6 subtests, $N = 645$) was 0.00 with a standard deviation of 1.00; for $n = 50$, the grand mean was 0.07 with a standard deviation of 1.03; for $n = 25$, the grand mean of was 0.09 with a standard deviation of 1.06; and for $n = 20$, the grand mean was 0.29 with a standard deviation of 1.01. Someone might ask why $B=500$ worked well to replicate the original factor structure for the sample sizes $n = 50$ and $n = 20$, but not for $n = 25$. This question requires investigation. Future research is required regarding this matter.

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Table 1

WPPSI-III Intelligence Subtests Intercorrelations: Ages From 5 To 7 Years Old (N = 645)

	SI	VC	WC	BD	MR	PCO
Similarities	1.00	0.66	0.60	0.44	0.42	0.40
Vocabulary	0.66	1.00	0.63	0.41	0.41	0.39
Word Context	0.60	0.63	1.00	0.41	0.41	0.40
Block Design	0.44	0.41	0.41	1.00	0.49	0.37
Matrix Reasoning	0.42	0.41	0.41	0.49	1.00	0.40
Picture Concepts	0.40	0.39	0.40	0.37	0.40	1.00

Table 2

Coordinates from One-Dimensional Nonmetric Solution and from the Second PrincipalComponent based on Intercorrelations of Intelligence Subtests

Subtests	Dimension	2 nd PC
Similarities	-1.00	-0.33
Vocabulary	-1.00	-0.41
Word Context	-1.00	-0.37
Block Design	1.01	0.47
Matrix Reasoning	1.01	0.51
Picture Concepts	0.99	0.32

Table 3

Coordinates of 2nd Principal Component including Bootstrapping Estimates

Subtests	<i>N</i> = 645	<i>n</i> = 50	<i>Bn</i> = 50	<i>n</i> = 25	<i>Bn</i> = 25	<i>n</i> = 20	<i>Bn</i> = 20
Similarities	-0.33	-0.33	-0.34	-0.15	-0.38	-0.44	-0.45
Vocabulary	-0.41	-0.29	-0.25	0.08	-0.65	-0.64	-0.60
Word Context	-0.37	-0.21	-0.40	-0.12	-0.05	0.21	-0.10
Block Design	0.47	0.09	0.12	-0.65	0.11	0.31	0.44
Matrix Reasoning	0.51	0.22	0.41	0.23	0.47	0.51	0.39
Picture Concepts	0.32	0.85	0.69	0.69	0.44	0.04	0.29

Table 4

Coordinates of MDS including Bootstrapping Estimates

Subtests	<i>N</i> = 645	<i>n</i> = 50	<i>Bn</i> = 50	<i>n</i> = 25	<i>Bn</i> = 25	<i>n</i> = 20	<i>Bn</i> = 20
Similarities	-1.00	-0.70	-1.03	-0.32	-0.42	-0.50	-1.15
Vocabulary	-1.00	-0.68	-0.64	-0.01	-1.85	-1.63	-1.22
Word Context	-1.00	-0.57	-0.97	-0.21	-0.33	-0.28	-0.02
Block Design	1.01	-0.11	0.23	1.65	0.75	1.31	1.72
Matrix Reasoning	1.01	-0.11	0.66	0.49	0.83	1.13	0.48
Picture Concepts	0.99	2.17	1.75	1.70	1.01	-0.02	0.18

Figure Captions

Figure 1. Path Diagram for The Model Using the Original Sample ($N = 645$)

Figure 2. Path Diagram for The Model Using the Bootstrapped Sample ($n = 50$)

Figure 3. Path Diagram for The Model Using the Bootstrapped Sample ($n = 25$)

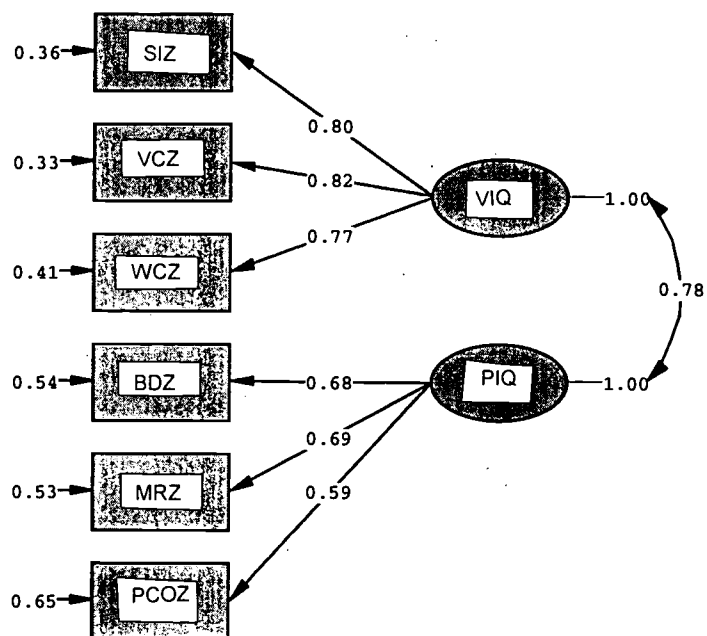
Figure 4. Path Diagram for The Model Using the Bootstrapped Sample ($n = 20$)

Figure 5. PC Profile Patterns of Non-Bootstrapped Samples

Figure 6. PC Profile Patterns of Bootstrapped Samples

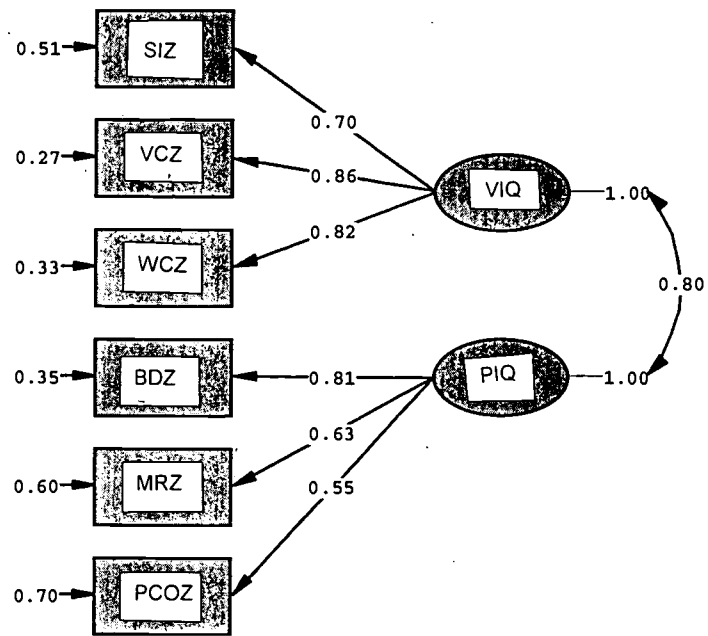
Figure 7. MDS Profile Patterns of Non-Bootstrapped Samples

Figure 8. MDS Profile Patterns of Bootstrapped Samples



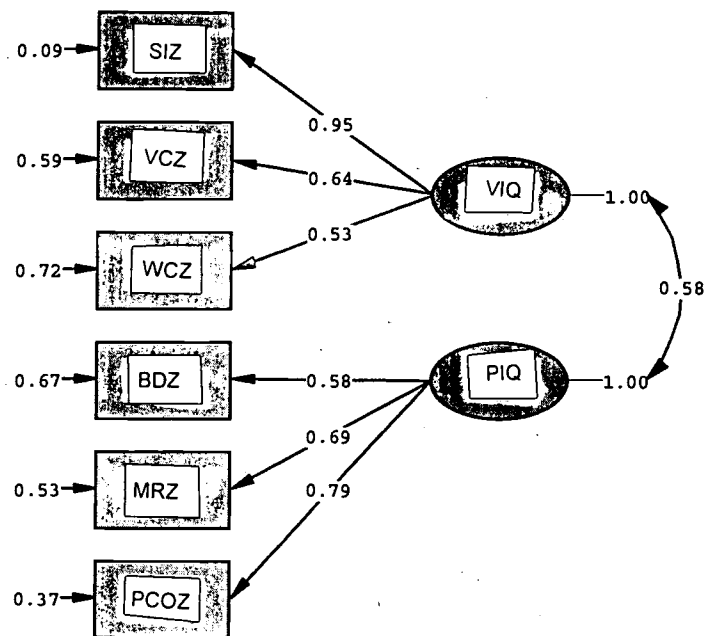
Chi-Square=10.84, df=8, P-value=0.21105, RMSEA=0.023

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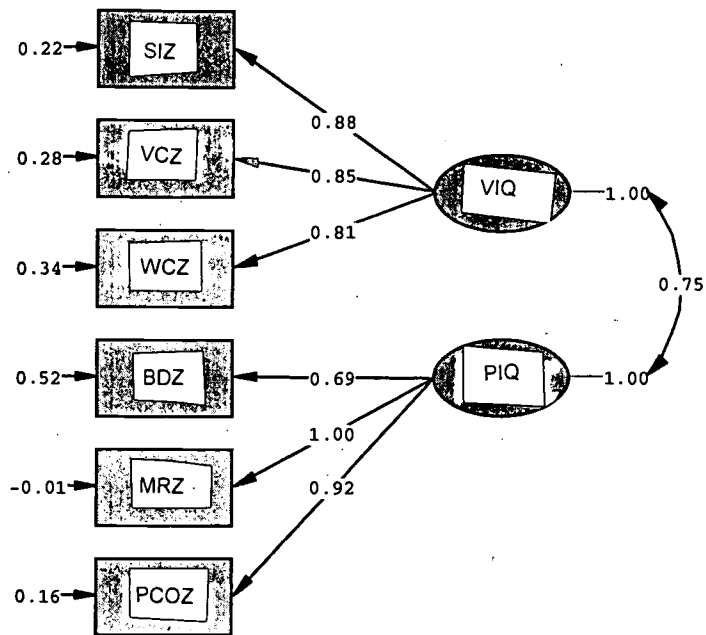
Chi-Square=3.61, df=8, P-value=0.89065, RMSEA=0.000

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Chi-Square=16.34, df=8, P-value=0.03774, RMSEA=0.208

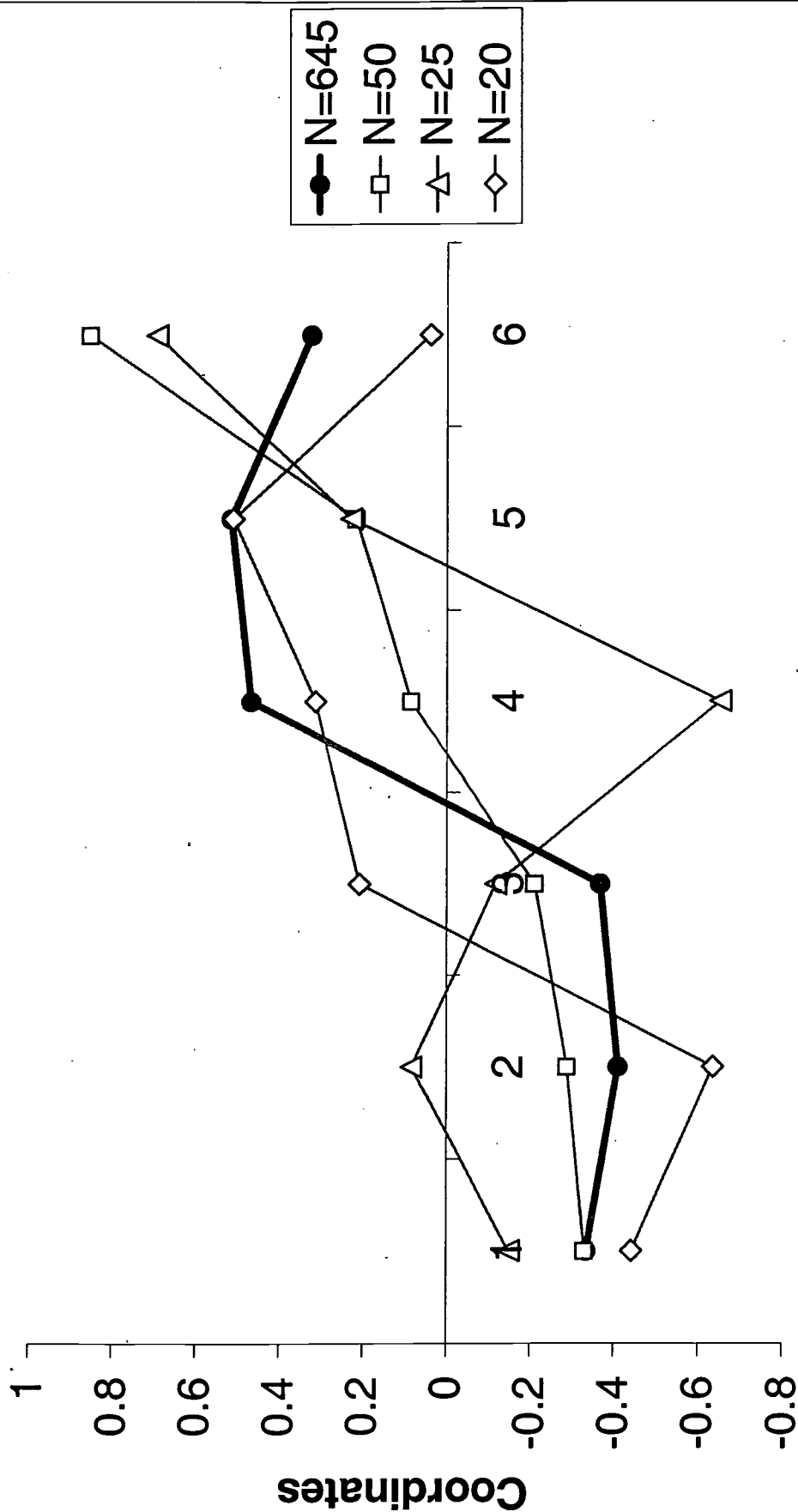
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Chi-Square=8.57, df=8, P-value=0.37994, RMSEA=0.061

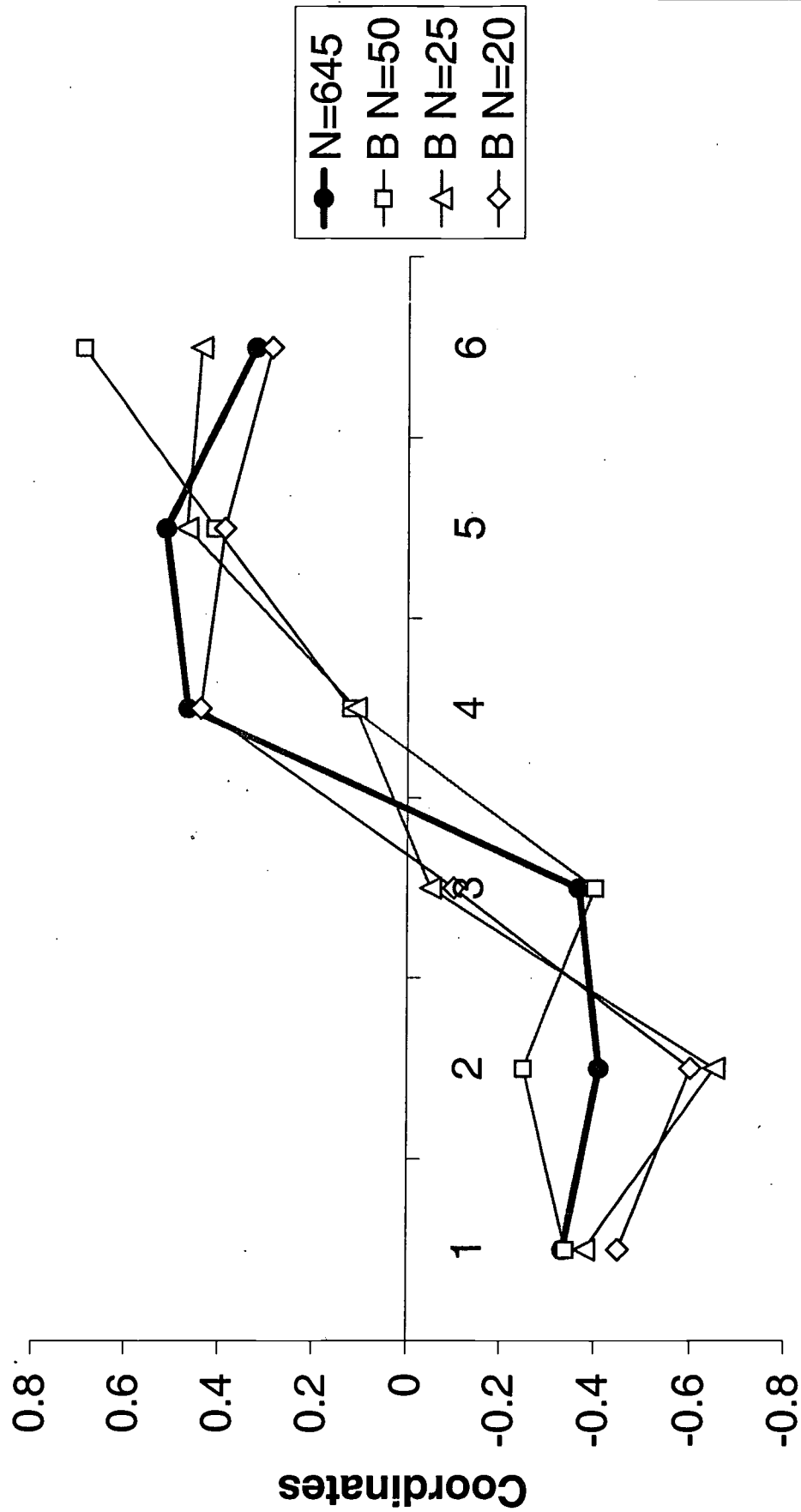
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PC Profile Patterns



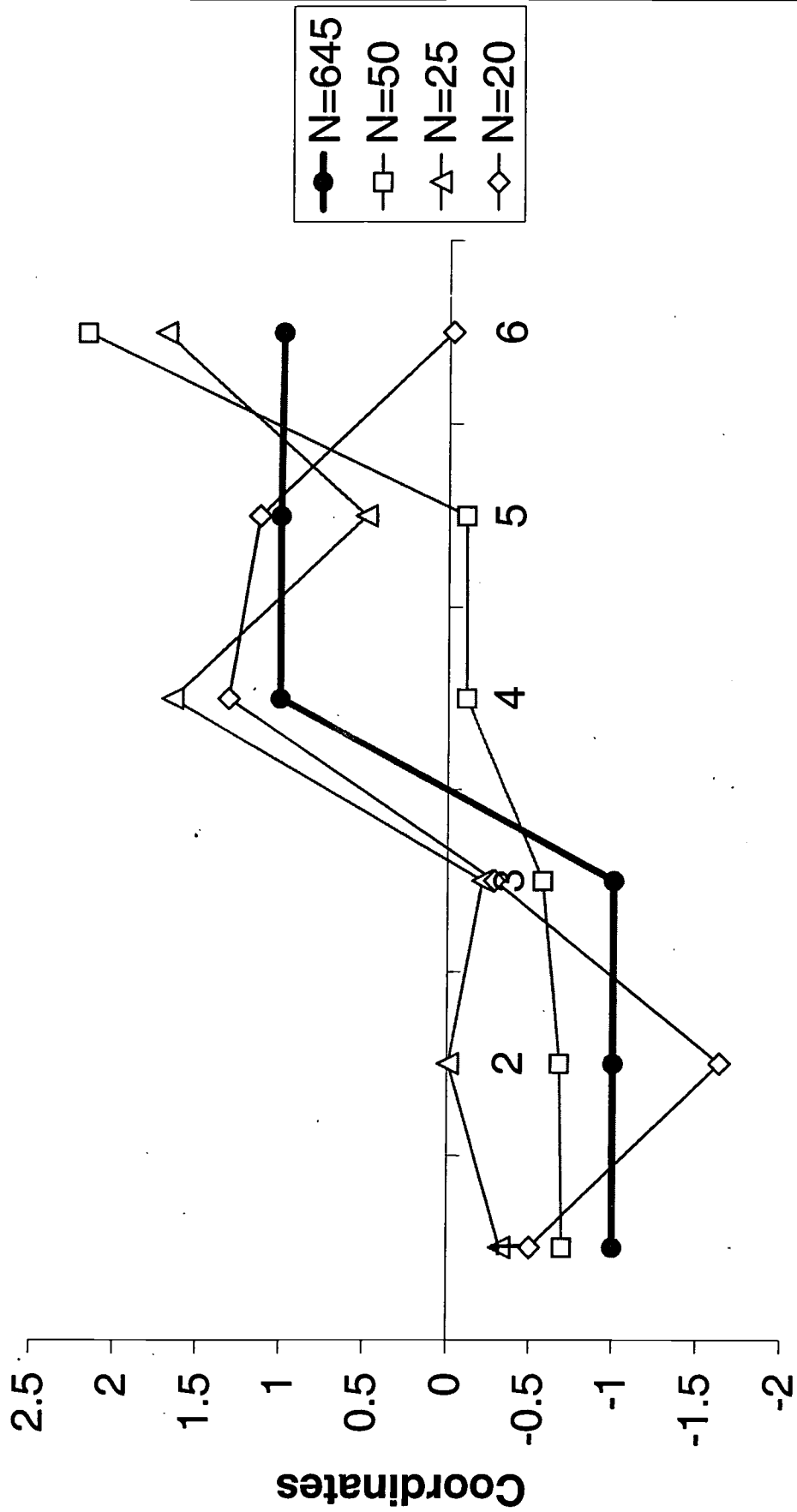
WPPSI-III Subtests (r=.52)

PC Profile Patterns (after BT)



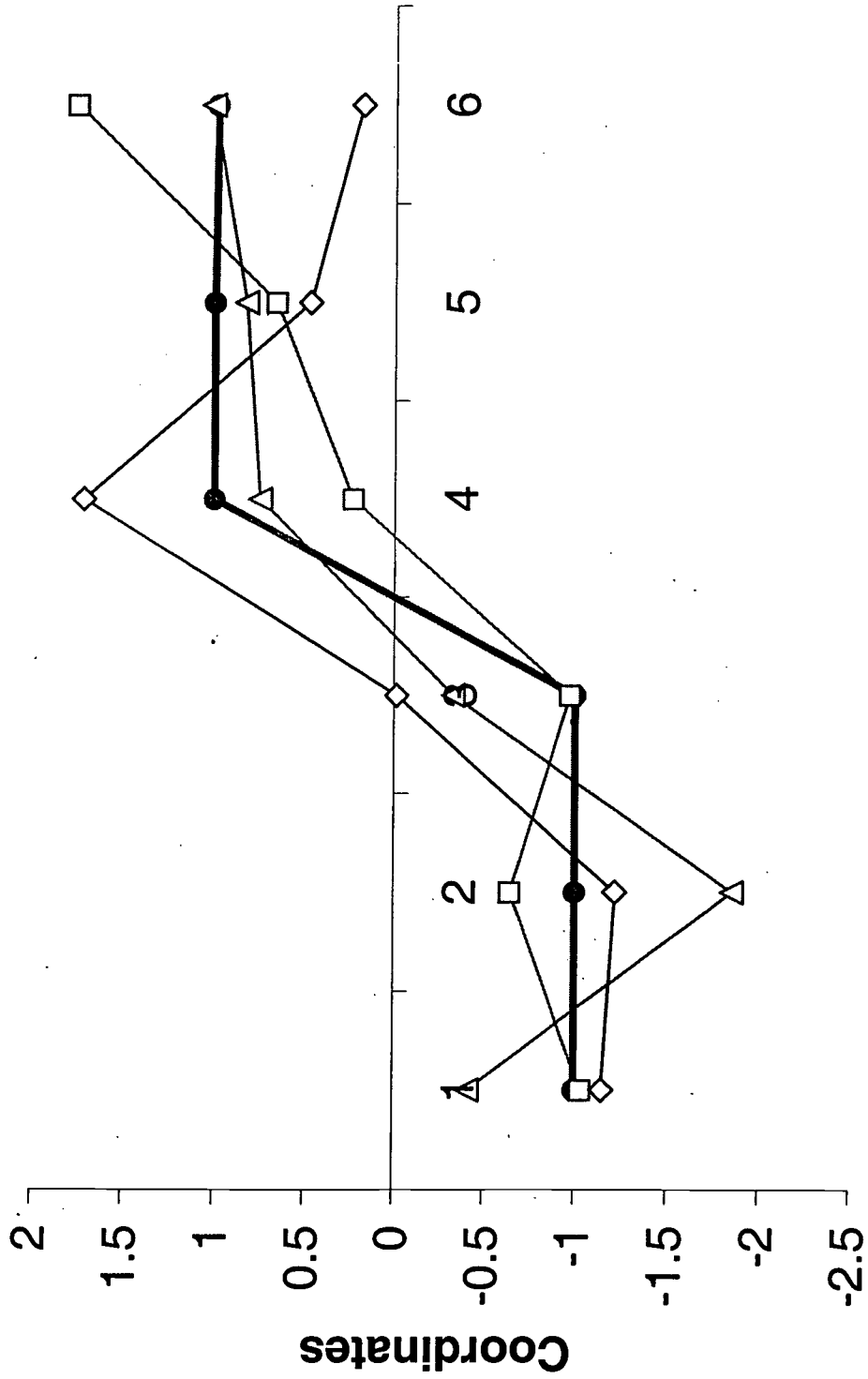
WPPSI-III Subtests ($r=.88$)

MDS Profile Patterns



WPPSI-III Subtests (r=.08)

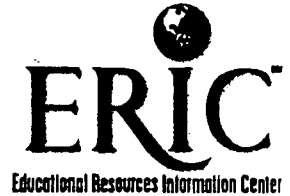
MDS Profile Patterns (after BT)



WPPSI-III Subtests (r=.85)



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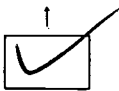
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